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**tt**

***Release 0.6.2***

**Jun 10, 2017**



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Welcome to the documentation site for tt.

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**Warning:** tt is heavily tested and fully usable, but is still pre-1.0/stable software with **no guarantees** of avoiding breaking API changes until hitting version 1.0.



# CHAPTER 1

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## Synopsis

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tt is a library aiming to provide a Pythonic toolkit for working with Boolean expressions. Please check out the [project site](#) for more information.





## CHAPTER 2

---

### Installation

---

tt is tested on CPython 2.7, 3.3, 3.4, 3.5, and 3.6. You can get the latest release from PyPI with:

```
pip install ttable
```



tt lets you do a few things with your prized Boolean expressions. Let's start by parsing one:

```
>>> from tt import BooleanExpression
>>> b = BooleanExpression('A impl not (B nand C)')
>>> b.tokens
['A', 'impl', 'not', '(', 'B', 'nand', 'C', ')']
>>> b.symbols
['A', 'B', 'C']
>>> print(b.tree)
impl
`----A
`----not
     `----nand
          `----B
          `----C
```

Then transform it a couple of times:

```
>>> from tt import apply_de_morgans, to_cnf, to_primitives
>>> b = to_primitives(b)
>>> b
<BooleanExpression "not A or not (not B or not C)">
>>> b = apply_de_morgans(b)
>>> b
<BooleanExpression "not A or (not not B and not not C)">
>>> b = to_cnf(b)
>>> b
<BooleanExpression "(not A or B) and (not A or C)">
```

Poke around its structure:

```
>>> b.is_cnf
True
>>> b.is_dnf
False
```

```
>>> for clause in b.iter_clauses():
...     print(clause)
...
not A or B
not A or C
```

Find all of its SAT solutions:

```
>>> for sat_solution in b.sat_all():
...     print(sat_solution)
...
A=0, B=1, C=1
A=0, B=1, C=0
A=0, B=0, C=1
A=0, B=0, C=0
A=1, B=1, C=1
```

Or just find one:

```
>>> with b.constrain(A=1):
...     b.sat_one()
...
<BooleanValues [A=1, B=1, C=1]>
```

Turn it into a truth table:

```
>>> from tt import TruthTable
>>> t = TruthTable(b)
>>> print(t)
+---+---+---+---+
| A | B | C |   |
+---+---+---+---+
| 0 | 0 | 0 | 1 |
+---+---+---+---+
| 0 | 0 | 1 | 1 |
+---+---+---+---+
| 0 | 1 | 0 | 1 |
+---+---+---+---+
| 0 | 1 | 1 | 1 |
+---+---+---+---+
| 1 | 0 | 0 | 0 |
+---+---+---+---+
| 1 | 0 | 1 | 0 |
+---+---+---+---+
| 1 | 1 | 0 | 0 |
+---+---+---+---+
| 1 | 1 | 1 | 1 |
+---+---+---+---+
```

And compare it to another truth table:

```
>>> other_table = TruthTable(from_values='111x00x1')
>>> other_table.ordering
['A', 'B', 'C']
>>> for inputs, result in other_table:
...     print(inputs, '=>', result)
...
A=0, B=0, C=0 => True
```

```
A=0, B=0, C=1 => True
A=0, B=1, C=0 => True
A=0, B=1, C=1 => x
A=1, B=0, C=0 => False
A=1, B=0, C=1 => False
A=1, B=1, C=0 => x
A=1, B=1, C=1 => True
>>> other_table.equivalent_to(t)
True
```



tt uses the MIT License.

## User Guide

Exploring the topics listed below should give you an idea of how to use the tools provided in this library. If anything remains unclear, please feel free to open an [issue on GitHub](#) or reach out to *the author*.

### Expression basics

At tt's core is the concept of the Boolean expression, encapsulated in this library with the *BooleanExpression* class. Let's take look at what we can do with expressions.

#### Creating an expression object

The top-level class for interacting with boolean expressions in tt is, fittingly named, *BooleanExpression*. Let's start by importing it:

```
>>> from tt import BooleanExpression
```

This class accepts boolean expressions as strings and provides the interface for parsing and tokenizing string expressions into a sequence of tokens and symbols, as we see here:

```
>>> b = BooleanExpression('(A nand B) or (C and D)')
>>> b.tokens
['(', 'A', 'nand', 'B', ')', 'or', '(', 'C', 'and', 'D', ')']
>>> b.symbols
['A', 'B', 'C', 'D']
```

We can also always retrieve the original string we passed in via the `raw_expr` attribute:

```
>>> b.raw_expr
'(A nand B) or (C and D)'
```

During initialization, the *BooleanExpression* also does some work behind the scenes to build a basic understanding of the expression's structure. It re-orders the tokens into postfix order, and uses this representation to build a *ExpressionTreeNode*. We can see this with:

```
>>> b.postfix_tokens
['A', 'B', 'nand', 'C', 'D', 'and', 'or']
>>> print(b.tree)
or
`----nand
|   `----A
|   `----B
`----and
     `----C
     `----D
```

This expression tree represents tt's understanding of the structure of your expression. If you are receiving an unexpected error for a more complicated expression, inspecting the `tree` attribute on the *BooleanExpression* instance can be a good starting point for debugging the issue.

## Evaluating expressions

Looking at expression symbols and tokens is nice, but we need some real functionality for our expressions; a natural starting point is the ability to evaluate expressions. A *BooleanExpression* object provides an interface to this evaluation functionality; use it like this:

```
>>> b.evaluate(A=True, B=False, C=True, D=False)
True
>>> b.evaluate(A=1, B=0, C=1, D=0)
True
```

Notice that we can use 0 or `False` to represent low values and 1 or `True` to represent high values. tt makes sure that only valid Boolean-esque values are accepted for evaluation. For example, if we tried something like:

```
>>> b.evaluate(A=1, B='not a Boolean value', C=0, D=0)
Traceback (most recent call last):
...
tt.errors.evaluation.InvalidBooleanValueError: "not a Boolean value" passed as value_
↳for "B" is not a valid Boolean value
```

or if we didn't include a value for each of the symbols:

```
>>> b.evaluate(A=1, B=0, C=0)
Traceback (most recent call last):
...
tt.errors.symbols.MissingSymbolError: Did not receive value for the following_
↳symbols: "D"
```

These exceptions can be nice if you aren't sure about your input, but if you think this safety is just adding overhead for you, there's a way to skip those extra checks:

```
>>> b.evaluate_unchecked(A=0, B=0, C=1, D=0)
True
```



## Handling malformed expressions

So far, we've only seen one example of a *BooleanExpression* instance, and we passed a valid expression string to it. What happens when we pass in a malformed expression? And what does tt even consider to be a malformed expression?

While there is no explicit grammar for expressions in tt, using your best judgement will work most of the time. Most well-known Boolean expression operators are available in plain-English and symbolic form. You can see the list of available operators like so:

```
>>> from tt import OPERATOR_MAPPING
>>> print(', '.join(sorted(OPERATOR_MAPPING.keys())))
!, &, &&, ->, /\, <->, AND, IFF, IMPL, NAND, NOR, NOT, NXOR, OR, XNOR, XOR, \/, and, &
->iff, impl, nand, nor, not, nxor, or, xnor, xor, |, ||, ~
```

Another possible source of errors in your expressions will be invalid symbol names. Due to some functionality based on accessing symbol names from *namedtuple*-like objects, symbol names must meet the following criteria:

1. Must be a valid Python identifiers.
2. Cannot be a Python keyword.
3. Cannot begin with an underscore

An exception will be raised if a symbol name in your expression does not meet the above criteria. Fortunately, tt provides a way for us to check if our symbols are valid. Let's take a look:

```
>>> from tt import is_valid_identifier
>>> is_valid_identifier('False')
False
>>> is_valid_identifier('_bad')
False
>>> is_valid_identifier('not$good')
False
>>> is_valid_identifier('a_good_symbol_name')
True
>>> b = BooleanExpression('_A or B')
Traceback (most recent call last):
...
tt.errors.grammar.InvalidIdentifierError: Invalid operand name "_A"
```

As we saw in the above example, we caused an error from the `tt.errors.grammar` module. If you play around with invalid expressions, you'll notice that all of these errors come from that module; that's because errors in this logical group are all descendants of *GrammarError*. This is the type of error that lexical expression errors will fall under:

```
>>> from tt import GrammarError
>>> invalid_expressions = ['A xor or B', 'A or ((B nand C)', 'A or B B']
>>> for expr in invalid_expressions:
...     try:
...         b = BooleanExpression(expr)
...     except Exception as e:
...         print(type(e))
...         print(isinstance(e, GrammarError))
...
<class 'tt.errors.grammar.ExpressionOrderError'>
True
<class 'tt.errors.grammar.UnbalancedParenError'>
True
```

```
<class 'tt.errors.grammar.ExpressionOrderError'>
True
```

*GrammarError* is a unique type of exception in tt, as it provides attributes for accessing the specific position in the expression string that caused an error. This is best illustrated with an example:

```
>>> try:
...     b = BooleanExpression('A or or B')
... except GrammarError as e:
...     print("Here's what happened:")
...     print(e.message)
...     print("Here's where it happened:")
...     print(e.expr_str)
...     print(' '*e.error_pos + '^')
...
Here's what happened:
Unexpected binary operator "or"
Here's where it happened:
A or or B
   ^
```

## Table basics

Truth tables are a nice way of showing the behavior of an expression for each permutation of possible inputs and are a nice tool to pair with expressions. Let's examine the interface provided by tt for working with truth tables.

### Creating a table object from an expression

Surprisingly, the top-level class for dealing with truth tables in tt is called *TruthTable*. Let's begin by importing it:

```
>>> from tt import TruthTable
```

There are a few ways we can fill up a truth table in tt. One of them is to pass in an expression, either as an already-created *BooleanExpression* object or as a string:

```
>>> t = TruthTable('A xor B')
>>> print(t)
+---+---+---+
| A | B |   |
+---+---+---+
| 0 | 0 | 0 |
+---+---+---+
| 0 | 1 | 1 |
+---+---+---+
| 1 | 0 | 1 |
+---+---+---+
| 1 | 1 | 0 |
+---+---+---+
```

As we saw in the above example, printing tables produces a nicely-formatted text table. Tables will scale to fit the size of the symbol names, too:

```
>>> t = TruthTable('operand_1 and operand_2')
>>> print(t)
+-----+-----+---+
```

```

| operand_1 | operand_2 |   |
+-----+-----+---+
|     0     |     0     | 0 |
+-----+-----+---+
|     0     |     1     | 0 |
+-----+-----+---+
|     1     |     0     | 0 |
+-----+-----+---+
|     1     |     1     | 1 |
+-----+-----+---+

```

By default, tt will order the symbols in the top row of the table to match the order of their appearance in the original expression; however, you can impose your own order, too:

```

>>> t = TruthTable('A xor B', ordering=['B', 'A'])
>>> print(t)
+---+---+---+
| B | A |   |
+---+---+---+
| 0 | 0 | 0 |
+---+---+---+
| 0 | 1 | 1 |
+---+---+---+
| 1 | 0 | 1 |
+---+---+---+
| 1 | 1 | 0 |
+---+---+---+

```

### Creating a table object from values

The tables we looked at above were populated by evaluating the expression for each combination of input values, but let's say that you already have the values you want in your truth table. You'd populate your table like this:

```

>>> t = TruthTable(from_values='00x1')
>>> print(t)
+---+---+---+
| A | B |   |
+---+---+---+
| 0 | 0 | 0 |
+---+---+---+
| 0 | 1 | 0 |
+---+---+---+
| 1 | 0 | x |
+---+---+---+
| 1 | 1 | 1 |
+---+---+---+

```

Notice that populating tables like this allows for *don't cares* (indicated by 'x') to be present in your table. Additionally, we can see that symbol names were automatically generated for us. That's nice sometimes, but what if we want to specify them ourselves? We return to the `ordering` keyword argument:

```

>>> t = TruthTable(from_values='1x01', ordering=['op1', 'op2'])
>>> print(t)
+-----+-----+---+
| op1 | op2 |   |
+-----+-----+---+

```

```

| 0 | 0 | 1 |
+---+---+---+
| 0 | 1 | x |
+---+---+---+
| 1 | 0 | 0 |
+---+---+---+
| 1 | 1 | 1 |
+---+---+---+

```

### Accessing values from a table

So far, we've only been able to examine the results stored in our tables by printing them. This is nice for looking at an end result, but we need programmatic methods of accessing the values in our tables. There's a few ways to do this in tt; one such example is the `results` attribute present on `TruthTable` objects, which stores all results in the table:

```

>>> t = TruthTable('!A && B')
>>> t.results
[False, True, False, False]

```

Results in the table are also available by indexing the table:

```

>>> t[0], t[1], t[2], t[3]
(False, True, False, False)

```

Accessing results by index is also an intuitive time to use binary literals:

```

>>> t[0b00], t[0b01], t[0b10], t[0b11]
(False, True, False, False)

```

Tables in tt are also iterable. There are a couple of important items to note. First, iterating through the entries in a table will skip over the entries that would have appeared as `None` in the `results` list. Second, in addition to the result, each iteration through the table yields a `namedtuple`-like object representing the inputs associated with that result. Let's take a look:

```

>>> for inputs, result in t:
...     inputs.A, inputs.B
...     str(inputs), result
...
(False, False)
('A=0, B=0', False)
(False, True)
('A=0, B=1', True)
(True, False)
('A=1, B=0', False)
(True, True)
('A=1, B=1', False)

```

### Partially filling tables

Up to this point, we've only taken a look at tables with all of their results filled in, but we don't have to completely fill up our tables to start working with them. Here's an example of iteratively filling a table:

```

>>> t = TruthTable('A nor B', fill_all=False)
>>> t.is_full

```

```

False
>>> print(t)
Empty!
>>> t.fill(A=0)
>>> t.is_full
False
>>> print(t)
+---+---+---+
| A | B |   |
+---+---+---+
| 0 | 0 | 1 |
+---+---+---+
| 0 | 1 | 0 |
+---+---+---+
>>> t.fill()
>>> t.is_full
True
>>> print(t)
+---+---+---+
| A | B |   |
+---+---+---+
| 0 | 0 | 1 |
+---+---+---+
| 0 | 1 | 0 |
+---+---+---+
| 1 | 0 | 0 |
+---+---+---+
| 1 | 1 | 0 |
+---+---+---+

```

Empty slots in the table will be represented with a corresponding `None` entry for their result:

```

>>> t = TruthTable('A or B', fill_all=False)
>>> t.results
[None, None, None, None]
>>> t.fill(B=0)
>>> t.results
[False, None, True, None]

```

Make sure not to try to keep filling an already-full table, though:

```

>>> t = TruthTable(from_values='0110')
>>> t.is_full
True
>>> t.fill()
Traceback (most recent call last):
...
tt.errors.state.AlreadyFullTableError: Cannot fill an already-full table

```

## Logical equivalence

Another neat feature provided by tt's tables is the checking of logical equivalence:

```

>>> t1 = TruthTable('A xor B')
>>> t2 = TruthTable(from_values='0110')
>>> t1.equivalent_to(t2)

```

```
True
>>> t1.equivalent_to('C xor D')
True
```

Note that this equivalence comparison looks only at the result values of the tables and doesn't examine at the symbols of either table.

Next, let's examine how *don't cares* function within tt's concept of logical equivalence. *Don't cares* in the calling table will be considered to equal to any value in the comparison table, but any explicit value in the calling table must be matched in the comparison table to be considered equal.

In this sense, a fully-specified table (i.e., one without any *don't cares*) will never be logically equivalent to one which contains *don't cares*, but the converse may be true. Let's see an example:

```
>>> t1 = TruthTable('C nand D')
>>> t2 = TruthTable(from_values='xx10')
>>> t1.equivalent_to(t2)
False
>>> t2.equivalent_to(t1)
True
```

The user guide is a work in progress, with more to come soon!

## Release Notes

Check below for new features added in each release. Please note that release notes were not recorded before version 0.5.0.

### 0.6.x

Features in the 0.6.x series of releases are focused on expanding functionality to include expression satisfiability and transformations.

#### 0.6.2

- Remove class `BooleanExpressionTree` in favor of working exclusively with instances of `ExpressionTreeNode`
- Add `AlreadyConstrainedSymbolError`
- Add `sat_all` to `picosat` interface
- Add `constrain`, `sat_one`, and `sat_all` to `BooleanExpression`
- Move the implementation logic of the `to_cnf` transformation to the `to_cnf` method of the `ExpressionTreeNode` class

#### 0.6.1

- Add `iff` (`iff`, `->`) and `implies` (`impl`, `<->`) Boolean operators
- Add `is_cnf` and `is_dnf` attributes to `BooleanExpression`

- Add functionality to initialize *BooleanExpression* objects from instances of *ExpressionTreeNode* or *BooleanExpressionTree*
- Update `__str__` and `__repr__` for *BooleanExpression*
- Add *is\_really\_unary* attribute to *ExpressionTreeNode*
- Add *iter\_clauses*, *iter\_cnf\_clauses*, and *iter\_dnf\_clauses* to *ExpressionTreeNode*
- Add *iter\_clauses*, *iter\_cnf\_clauses*, and *iter\_dnf\_clauses* to *BooleanExpression*
- Add *RequiresNormalFormError*
- Add attributes *default\_symbol\_str* and *default\_plain\_english\_str* to *BooleanOperator*, in place of removed name attribute
- Add *to\_primitives*, *coalesce\_negations*, *distribute\_and*s, *distribute\_or*s, and *apply\_de\_morgans* to *ExpressionTreeNode*
- Introduce high-level *transformations* interface, including transformation functions *to\_primitives*, *coalesce\_negations*, *distribute\_and*s, *distribute\_or*s, *to\_cnf*, and *apply\_de\_morgans*
- Add *BINARY\_OPERATORS* and *NON\_PRIMITIVE\_OPERATORS* sets to *definitions* module
- Add `__eq__` and `__ne__` implementations for *BooleanExpression* and derivatives of *ExpressionTreeNode*

## 0.6.0

- Add *is\_valid\_identifier* helper method for checking if symbol names are valid
- Add checking of valid symbol names to *BooleanExpression* and *TruthTable* initialization logic, with corresponding new exception type *InvalidIdentifierError*
- Add *boolean\_variables\_factory* helper for generating more intuitive collections of symbol inputs
- Update `__iter__` in *TruthTable* to yield inputs as a *namedtuple*-like object rather than a plain *tuple*
- Re-organize *User Guide* into different sections instead of one long page
- Remove PyPy support, due to addition of C-extensions
- Add OS X builds to Travis
- Include both 32-bit and 64-bit builds on AppVeyor
- Add initial wrapper around *PicoSAT* library for future satisfiability interface; namely, the *sat\_one* method
- Add automated deployment to PyPI on tagged commits from CI services

## 0.5.x

Features in the 0.5.x series of releases were focused on expanding the top-level interface and improving optimizations under the hood. See below for specific features and fixes.

### 0.5.1

- Add *from\_values* option to the *TruthTable* initializer, allowing for table creation directly from values
- Add ability to store *don't cares* in a *TruthTable*

- Add `equivalent_to` method to `TruthTable` to check for equivalence of sources of truth
- Convert `generate_symbols` and `input_combos` to be static methods of the `TruthTable` class
- Add `is_full` to `TruthTable`
- Add `__iter__` and `__getitem__` functionality to `TruthTable`
- Add nice-looking `__str__` to `BooleanExpression`
- Add new exception types: `AlreadyFullTableError`, `ConflictingArgumentsError`, and `RequiredArgumentError`
- Re-organize exception hierarchy so each group of exceptions extends from the same base class
- Re-organize the test file structure into more-focused files
- Add *User Guide*, acting as tutorial-style documentation
- Remove CLI example from the README
- Update documentation color palette

### 0.5.0

- Added the Release Notes section to the project's documentation (how fitting for this page)
- Publically exposed the `input_combos` method in the `TruthTable` class
- Added test coverage for the CPython 3.6, PyPy, and PyPy3 runtimes
- Migrated all documentation to from `Napoleon` docstrings to standard `Sphinx` docstrings
- Added `doctest` tests to the documentation
- Added type-checking to the `BooleanExpression` class's initialization
- Fixed a bug in the handling of empty expressions in the CLI

### pre-0.5

Unfortunately, release notes were not kept before the 0.5.0 release.

## Development

If you'd like to help out with `tt`, we'd love to have you. Below are some helpful tips to development. Feel free to *reach out* with any questions about development or getting involved.

### Managing with `ttasks.py`

`tt` ships with a script `ttasks.py` (`tt + tasks = ttasks`) in the project's top-level directory, used to manage common project tasks such as running tests, building the docs, and serving the docs via a live-reload server. You will see this script referenced below.



## Dependencies

All development requirements for tt are stored in the `dev-requirements.txt` file in the project's top-level directory. You can install all of these dependencies with:

```
pip install -r dev-requirements.txt
```

## Testing

Testing is done with Python's `unittest` and `doctest` modules. All tests can be run using the `ttasks.py` script:

```
python ttasks.py test
```

Note that while doc tests are used, this is mostly just to make sure the documentation examples are valid. The true behavior of the library and its public contract are enforced through the unit tests.

Cross-Python version testing is achieved through `tox`. To run changes against the reference and style tests, simply invoke `tox` from the top-level directory of the project; `tox` will run the unit tests against the compatible CPython runtimes. Additionally, the source is run through the `Flake8` linter. Whenever new code is pushed to the repo, this same set of `tox` tests is run on `AppVeyor` (for Windows builds). A separate configuration is used for `Travis CI`, which tests on Linux.

## Coding Style

tt aims to be strictly `PEP8` compliant, enforcing this compliance via `Flake8`. This project also includes an `editorconfig` file to help with formatting issues.

## Documentation

To build the docs from source, run the following:

```
python ttasks.py build-docs
```

If you're going to be working for a little bit, it's usually more convenient to boot up a live-reload server that will re-build the docs on any source file changes. To run one on port 5000 of your machine, run:

```
python ttasks.py serve-docs
```

## Building C-extensions

tt contains some C-extensions that need to be built before the library is fully usable. They can be built and installed in a development environment by running:

```
python setup.py build
python setup.py develop
```

from the project's top-level directory. There are some dependencies required for compiling these extensions, which can be a little difficult to get up and running on Windows. You will need to install several different compilers:

- `Microsoft Visual C++ 9.0` (for Python 2.7)
- `Microsoft Visual C++ 10.0` (for Python 3.3 and 3.4)

- [Microsoft Visual C++ 14.0](#) (for Python 3.5 and 3.6)

For reference, check out this [comprehensive list of Windows compilers](#) necessary for building Python and C-extensions. You may have some trouble installing the 7.1 SDK (which contains Visual C++ 10.0). [This stackoverflow answer](#) provides some possible solutions.

## Releases

Work for each release is done in a branch off of develop following the naming convention `v{major}.{minor}.{micro}`. When work for a version is complete, its branch is merged back into develop, which is subsequently merged into master. The master branch is then tagged with the release version number, following the scheme `{major}.{minor}.{micro}`.

Wheels for Windows environments are provided on PyPI. To get the built wheels from the release build on AppVeyor, make sure you have the `APPVEYOR_TOKEN` environment variable set and run:

```
python ttasks.py pull-latest-win-wheels
```

This should download the files into a `dist` folder in the top-level directory of the project. Once downloaded, you can upload the Wheels to PyPI with:

```
twine upload dist/*
```

## Prior Art

There are some great projects operating in the same problem space as tt and might be worth a look. Many of tt's design and feature choices were inspired by the libraries listed on this page. If you think that your library should be listed here, please let me know or submit a PR.

## General purpose EDA/Boolean logic

- [boolean.py](#)
- [PyEDA](#)
- [LogicNG](#) (Java)
- [BoolExpr](#) (C++)
- [EvalEx](#) (Java)

## Satisfiability

- [PyEDA](#)
- [pycosat](#)
- [SATisPy](#)

## Special Thanks

A lot of free services and open source libraries have helped this project become possible. This page aims to give credit where its due; if you were left out, I'm sorry! Please let me know!

## Services

Thank you to the free hosting provided by these services!

- [Github](#)
- [Travis CI](#)
- [AppVeyor](#)
- [Read the Docs](#)

## Design Resources

Thank you to Matthew Beckler, who designed the [logic gate SVGs](#) present in tt's logo.

## Third Party Libraries Shipped with tt

Thank you to the developers of the following third party libraries that are wrapped in and shipped with tt. Your hard work drives some of the most powerful functionality of tt.

- [PicoSAT](#)

## Inspiration

Thanks goes to the developers of the [PyEDA](#) and [pycosat](#) libraries, whose interface and design are inspirations behind a lot of the functionality packed in tt.

## Open Source Projects & Libraries

tt relies on some well-written and well-documented projects and libraries for its development, listed below. Thank you!

- [Alabaster](#)
- [Babel](#)
- [Colorama](#)
- [Docutils](#)
- [Flake8](#)
- [imagesize](#)
- [Jinja2](#)
- [MarkupSafe](#)
- [McCabe](#)
- [pep8](#)
- [pluggy](#)
- [py](#)
- [pyenv](#)
- [pyflakes](#)

- Pygments
- Python
- pytz
- Requests
- six
- snowballstemmer
- Sphinx
- tox
- virtualenv

## Author

tt is written by Brian Welch. If you'd like to discuss anything about this library, Python, or software engineering in general, please feel free to reach out via one of the below channels.

- [Personal website](#)
- [Github](#)

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Want to learn more?

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If you're just getting started and looking for tutorial-style documentation, head on over to the *User Guide*. If you would prefer a comprehensive view of this library's functionality, check out the API docs:

## cli

tt's command-line interface.

### cli.core module

Core command-line interface for tt.

`tt.cli.core.get_parsed_args` (*args=None*)

Get the parsed command line arguments.

**Parameters** `args` (*List[str], optional*) – The command-line args to parse; if omitted, `sys.argv` will be used.

**Returns** The `Namespace` object holding the parsed args.

**Return type** `argparse.Namespace`

`tt.cli.core.main` (*args=None*)

The main routine to run the tt command-line interface.

**Parameters** `args` (*List[str], optional*) – The command-line arguments.

**Returns** The exit code of the program.

**Return type** `int`

## cli.utils module

Utilities for the tt command-line interface.

```
tt.cli.utils.print_err(*args, **kwargs)
    A thin wrapper around print, explicitly printing to stderr.
tt.cli.utils.print_info(*args, **kwargs)
    A thin wrapper around print, explicitly printing to stdout.
```

## definitions

Definitions for tt's expression grammar, operands, and operators.

### definitions.grammar module

Definitions related to expression grammar.

```
tt.definitions.grammar.CONSTANT_VALUES = {'0', '1'}
    Set of tokens that act as constant values in expressions.
    Type Set[str]
tt.definitions.grammar.DELIMITERS = {' ', '(', ')'}
    Set of tokens that act as delimiters in expressions.
    Type Set[str]
```

### definitions.operands module

Definitions related to operands.

```
tt.definitions.operands.BOOLEAN_VALUES = {False, True}
    Set of truthy values valid to submit for evaluation.
    Type Set[int, bool]
tt.definitions.operands.DONT_CARE_VALUE = 'x'
    The don't care string identifier.
    Type str
tt.definitions.operands.boolean_variables_factory(symbols)
    Returns a class for namedtuple-like objects for holding boolean values.
    Parameters symbols (List[str]) – A list of the symbol names for which instances of this class
        will hold an entry.
    Returns An object where the passed symbols can be accessed as attributes.
    Return type namedtuple-like object
```

This functionality is best demonstrated with an example:

```
>>> from tt import boolean_variables_factory
>>> factory = boolean_variables_factory(['op1', 'op2', 'op3'])
>>> instance = factory(op1=True, op2=False, op3=False)
>>> instance.op1
```

```

True
>>> instance.op2
False
>>> print(instance)
op1=1, op2=0, op3=0
>>> instance = factory(op1=0, op2=0, op3=1)
>>> instance.op3
1
>>> print(instance)
op1=0, op2=0, op3=1

```

It should be noted that this function is used internally within functionality where the validity of inputs is already checked. As such, this class won't enforce the Boolean-ness of input values:

```

>>> factory = boolean_variables_factory(['A', 'B'])
>>> instance = factory(A=-1, B='value')
>>> print(instance)
A=-1, B=value

```

Instances produced from the generated factory are descendants of `namedtuple` generated classes; some of the inherited attributes may be useful:

```

>>> instance = factory(A=True, B=False)
>>> instance._fields
('A', 'B')
>>> instance._asdict()
OrderedDict([('A', True), ('B', False)])

```

`tt.definitions.operands.is_valid_identifier` (*identifier\_name*)

Returns whether the string is a valid symbol identifier.

Valid identifiers are those that follow Python variable naming conventions, are not Python keywords, and do not begin with an underscore.

**Parameters** `identifier_name` (`str`) – The string to test.

**Returns** True if the passed string is valid identifier, otherwise False.

**Return type** `bool`

**Raises**

- `InvalidArgumentTypeError` – If `identifier_name` is not a string.
- `InvalidArgumentValueError` – If `identifier_name` is an empty string.

As an example:

```

>>> from tt import is_valid_identifier
>>> is_valid_identifier('$var')
False
>>> is_valid_identifier('va#r')
False
>>> is_valid_identifier('for')
False
>>> is_valid_identifier('False')
False
>>> is_valid_identifier('var')
True
>>> is_valid_identifier('')

```

```

Traceback (most recent call last):
...
tt.errors.arguments.InvalidArgumentValueError: identifier_name cannot be empty
>>> is_valid_identifier(None)
Traceback (most recent call last):
...
tt.errors.arguments.InvalidArgumentTypeError: identifier_name must be a string

```

## definitions.operators module

Definitions for tt's built-in Boolean operators.

`tt.definitions.operators.BINARY_OPERATORS` = {<BooleanOperator "impl">, <BooleanOperator "xor">, <BooleanOperator "and">}

The set of all binary operators available in tt.

**Type** Set{*BooleanOperator*}

**class** `tt.definitions.operators.BooleanOperator` (*precedence*, *eval\_func*, *default\_symbol\_str*, *default\_plain\_english\_str*)

Bases: `object`

A thin wrapper around a Boolean operator.

**default\_plain\_english\_str**

The default plain English string representation of this operator.

Unlike *default\_symbol\_str*, this attribute should never be `None`.

**Type** `str`

```

>>> from tt.definitions import TT_AND_OP, TT_NAND_OP
>>> print(TT_AND_OP.default_plain_english_str)
and
>>> print(TT_NAND_OP.default_plain_english_str)
nand

```

**default\_symbol\_str**

The default symbolic string representation of this operator.

Some operators may not have a recognized symbol str, in which case this attribute will be `None`.

**Type** `str` or `None`

```

>>> from tt.definitions import TT_AND_OP, TT_NAND_OP
>>> print(TT_AND_OP.default_symbol_str)
/\
>>> print(TT_NAND_OP.default_symbol_str)
None

```

**eval\_func**

The evaluation function wrapped by this operator.

**Type** `Callable`

```

>>> from tt.definitions import TT_XOR_OP
>>> TT_XOR_OP.eval_func(0, 0)
False
>>> TT_XOR_OP.eval_func(True, False)
True

```



**precedence**

Precedence of this operator, relative to other operators.

**Type** *int*

```
>>> from tt.definitions import TT_AND_OP, TT_OR_OP
>>> TT_AND_OP.precedence > TT_OR_OP.precedence
True
```

`tt.definitions.operators.MAX_OPERATOR_STR_LEN = 4`

The length of the longest operator from *OPERATOR\_MAPPING*.

**Type** *int*

`tt.definitions.operators.NON_PRIMITIVE_OPERATORS = {<BooleanOperator “nor”>, <BooleanOperator “nand”>}`

The set of non-primitive operators available in tt.

This includes all binary operators other than AND and OR.

**Type** *Set{BooleanOperator}*

`tt.definitions.operators.OPERATOR_MAPPING = {'&&': <BooleanOperator “and”>, 'xor': <BooleanOperator “xor”>}`

A mapping of all available Boolean operators.

This dictionary is the concatenation of the *PLAIN\_ENGLISH\_OPERATOR\_MAPPING* and *SYMBOLIC\_OPERATOR\_MAPPING* dictionaries.

**Type** *Dict{str: BooleanOperator}*

`tt.definitions.operators.PLAIN_ENGLISH_OPERATOR_MAPPING = {'NXOR': <BooleanOperator “xnor”>, 'NAND': <BooleanOperator “nand”>}`

A mapping of Boolean operators.

This mapping includes the plain-English variants of the available Boolean operators.

**Type** *Dict{str: BooleanOperator}*

`tt.definitions.operators.SYMBOLIC_OPERATOR_MAPPING = {'&': <BooleanOperator “and”>, '!': <BooleanOperator “not”>}`

A mapping of Boolean operators.

This mapping includes the symbolic variants of the available Boolean operators.

**Type** *Dict{str: BooleanOperator}*

`tt.definitions.operators.TT_AND_OP = <BooleanOperator “and”>`

tt’s operator implementation of a Boolean AND.

**Type** *BooleanOperator*

`tt.definitions.operators.TT_IMPL_OP = <BooleanOperator “impl”>`

tt’s operator implementation of a Boolean IMPLIES.

**Type** *BooleanOperator*

`tt.definitions.operators.TT_NAND_OP = <BooleanOperator “nand”>`

tt’s operator implementation of a Boolean NAND.

**Type** *BooleanOperator*

`tt.definitions.operators.TT_NOR_OP = <BooleanOperator “nor”>`

tt’s operator implementation of a Boolean NOR.

**Type** *BooleanOperator*

`tt.definitions.operators.TT_NOT_OP = <BooleanOperator “not”>`

tt’s operator implementation of a Boolean NOT.

Type *BooleanOperator*

`tt.definitions.operators.TT_OR_OP = <BooleanOperator "or">`  
tt's operator implementation of a Boolean OR.

Type *BooleanOperator*

`tt.definitions.operators.TT_XNOR_OP = <BooleanOperator "xnor">`  
tt's operator implementation of a Boolean XNOR.

Type *BooleanOperator*

`tt.definitions.operators.TT_XOR_OP = <BooleanOperator "xor">`  
tt's operator implementation of a Boolean XOR.

Type *BooleanOperator*

## errors

tt error types.

### errors.base module

The base tt exception type.

**exception** `tt.errors.base.TtError` (*message*, \**args*)

Bases: *Exception*

Base exception type for tt errors.

---

**Note:** This exception type should be sub-classed and is not meant to be raised explicitly.

---

**message**

A helpful message intended to be shown to the end user.

Type `str`

### errors.arguments module

Generic exception types.

**exception** `tt.errors.arguments.ArgumentError` (*message*, \**args*)

Bases: *tt.errors.base.TtError*

An exception type for invalid arguments.

---

**Note:** This exception type should be sub-classed and is not meant to be raised explicitly.

---

**exception** `tt.errors.arguments.ConflictingArgumentsError` (*message*, \**args*)

Bases: *tt.errors.arguments.ArgumentError*

An exception type for two or more conflicting arguments.

```
>>> from tt import TruthTable
>>> try:
...     t = TruthTable('A or B', from_values='1111')
... except Exception as e:
...     print(type(e))
...
<class 'tt.errors.arguments.ConflictingArgumentsError'>
```

**exception** `tt.errors.arguments.InvalidArgumentTypeError` (*message*, \*args)  
Bases: `tt.errors.arguments.ArgumentError`

An exception type for invalid argument types.

```
>>> from tt import TruthTable
>>> try:
...     t = TruthTable(7)
... except Exception as e:
...     print(type(e))
...
<class 'tt.errors.arguments.InvalidArgumentTypeError'>
```

**exception** `tt.errors.arguments.InvalidArgumentValueError` (*message*, \*args)  
Bases: `tt.errors.arguments.ArgumentError`

An exception type for invalid argument values.

```
>>> from tt import TruthTable
>>> try:
...     t = TruthTable(from_values='01x')
... except Exception as e:
...     print(type(e))
...
<class 'tt.errors.arguments.InvalidArgumentValueError'>
```

**exception** `tt.errors.arguments.RequiredArgumentError` (*message*, \*args)  
Bases: `tt.errors.arguments.ArgumentError`

An exception for when a required argument is missing.

```
>>> from tt import TruthTable
>>> try:
...     t = TruthTable()
... except Exception as e:
...     print(type(e))
...
<class 'tt.errors.arguments.RequiredArgumentError'>
```

## errors.evaluation module

Exception type definitions related to expression evaluation.

**exception** `tt.errors.evaluation.EvaluationError` (*message*, \*args)  
Bases: `tt.errors.base.TtError`

An exception type for errors occurring in expression evaluation.

---

**Note:** This exception type should be sub-classed and is not meant to be raised explicitly.

---

**exception** `tt.errors.evaluation.InvalidBooleanValueError` (*message*, \**args*)

Bases: `tt.errors.evaluation.EvaluationError`

An exception for an invalid truth or don't care value passed.

```
>>> from tt import BooleanExpression
>>> try:
...     b = BooleanExpression('A or B')
...     b.evaluate(A=1, B='brian')
... except Exception as e:
...     print(type(e))
...
<class 'tt.errors.evaluation.InvalidBooleanValueError'>
```

**exception** `tt.errors.evaluation.NoEvaluationVariationError` (*message*, \**args*)

Bases: `tt.errors.evaluation.EvaluationError`

An exception type for when evaluation of an expression will not vary.

```
>>> from tt import TruthTable
>>> try:
...     t = TruthTable('1 or 0')
... except Exception as e:
...     print(type(e))
...
<class 'tt.errors.evaluation.NoEvaluationVariationError'>
```

## errors.grammar module

Exception type definitions related to expression grammar and parsing.

**exception** `tt.errors.grammar.BadParenPositionError` (*message*, *expr\_str=None*, *error\_pos=None*, \**args*)

Bases: `tt.errors.grammar.GrammarError`

An exception type for unexpected parentheses.

```
>>> from tt import BooleanExpression
>>> try:
...     b = BooleanExpression(') A or B')
... except Exception as e:
...     print(type(e))
...
<class 'tt.errors.grammar.BadParenPositionError'>
```

**exception** `tt.errors.grammar.EmptyExpressionError` (*message*, *expr\_str=None*, *error\_pos=None*, \**args*)

Bases: `tt.errors.grammar.GrammarError`

An exception type for when an empty expression is received.

```
>>> from tt import BooleanExpression
>>> try:
...     b = BooleanExpression('')
... except Exception as e:
```

```

...     print(type(e))
...
<class 'tt.errors.grammar.EmptyExpressionError'>

```

**exception** `tt.errors.grammar.ExpressionOrderError` (*message*, *expr\_str=None*, *error\_pos=None*, \*args)

Bases: `tt.errors.grammar.GrammarError`

An exception type for unexpected operands or operators.

```

>>> from tt import BooleanExpression
>>> try:
...     b = BooleanExpression('A or or B')
... except Exception as e:
...     print(type(e))
...
<class 'tt.errors.grammar.ExpressionOrderError'>

```

**exception** `tt.errors.grammar.GrammarError` (*message*, *expr\_str=None*, *error\_pos=None*, \*args)

Bases: `tt.errors.base.TtError`

Base type for errors that occur in the handling of expression.

---

**Note:** This exception type should be sub-classed and is not meant to be raised explicitly.

---

#### **error\_pos**

The position in the expression where the error occurred.

---

**Note:** This may be left as `None`, in which case there is no specific location in the expression causing the exception.

---

Type `int`

#### **expr\_str**

The expression in which the exception occurred.

---

**Note:** This may be left as `None`, in which case the expression will not be propagated with the exception.

---

Type `str`

**exception** `tt.errors.grammar.InvalidIdentifierError` (*message*, *expr\_str=None*, *error\_pos=None*, \*args)

Bases: `tt.errors.grammar.GrammarError`

An exception type for invalid operand names.

```

>>> from tt import BooleanExpression, TruthTable
>>> b = BooleanExpression('%A or B')
Traceback (most recent call last):
...
tt.errors.grammar.InvalidIdentifierError: Invalid operand name "%A"
>>> t = TruthTable(from_values='0x11', ordering=['A', 'while'])
Traceback (most recent call last):

```

```

...
tt.errors.grammar.InvalidIdentifierError: "while" in ordering is not a valid_
↳symbol name

```

**exception** `tt.errors.grammar.UnbalancedParenError` (*message*, *expr\_str=None*, *error\_pos=None*, \*args)

Bases: `tt.errors.grammar.GrammarError`

An exception type for unbalanced parentheses.

```

>>> from tt import BooleanExpression
>>> try:
...     b = BooleanExpression('A or ((B)')
... except Exception as e:
...     print(type(e))
...
<class 'tt.errors.grammar.UnbalancedParenError'>

```

## errors.state module

Exception type definitions related to invalid operations based on state.

**exception** `tt.errors.state.AlreadyConstrainedSymbolError` (*message*, \*args)

Bases: `tt.errors.state.StateError`

An exception to be raised when trying to doubly constrain a symbol.

```

>>> from tt import BooleanExpression
>>> b = BooleanExpression('A or B or C')
>>> with b.constrain(C=1):
...     with b.constrain(C=0):
...         pass
...
Traceback (most recent call last):
tt.errors.state.AlreadyConstrainedSymbolError: Symbol "C" cannot be constrained_
↳multiple times

```

**exception** `tt.errors.state.AlreadyFullTableError` (*message*, \*args)

Bases: `tt.errors.state.StateError`

An exception to be raised when attempting to fill an already-full table.

```

>>> from tt import TruthTable
>>> t = TruthTable('A or B', fill_all=False)
>>> t.fill()
>>> t.is_full
True
>>> t.fill()
Traceback (most recent call last):
tt.errors.state.AlreadyFullTableError: Cannot fill an already-full table

```

**exception** `tt.errors.state.RequiresFullTableError` (*message*, \*args)

Bases: `tt.errors.state.StateError`

An exception to be raised when a full table is required.

```
>>> from tt import TruthTable
>>> t = TruthTable('A or B', fill_all=False)
>>> t.equivalent_to('A or B')
Traceback (most recent call last):
tt.errors.state.RequiresFullTableError: Equivalence can only be checked on full_
↳truth tables
```

**exception** `tt.errors.state.RequiresNormalFormError` (*message*, \*args)

Bases: `tt.errors.state.StateError`

An exception to be raised when expression normal form is required.

```
>>> from tt import BooleanExpression
>>> b = BooleanExpression('A nand (B or C)')
>>> b.is_cnf or b.is_dnf
False
>>> for clause in b.iter_clauses():
...     print(clause)
...
Traceback (most recent call last):
tt.errors.state.RequiresNormalFormError: Must be in conjunctive or disjunctive_
↳normal form to iterate clauses
```

**exception** `tt.errors.state.StateError` (*message*, \*args)

Bases: `tt.errors.base.TtError`

Base exception type for errors involving invalid state.

## errors.symbols module

Exception types related to symbol processing.

**exception** `tt.errors.symbols.DuplicateSymbolError` (*message*, \*args)

Bases: `tt.errors.symbols.SymbolError`

An exception type for user-specified duplicate symbols.

```
>>> from tt import TruthTable
>>> try:
...     t = TruthTable('A or B', ordering=['A', 'A', 'B'])
... except Exception as e:
...     print(type(e))
...
<class 'tt.errors.symbols.DuplicateSymbolError'>
```

**exception** `tt.errors.symbols.ExtraSymbolError` (*message*, \*args)

Bases: `tt.errors.symbols.SymbolError`

An exception for a passed token that is not a parsed symbol.

```
>>> from tt import TruthTable
>>> try:
...     t = TruthTable('A or B', ordering=['A', 'B', 'C'])
... except Exception as e:
...     print(type(e))
...
<class 'tt.errors.symbols.ExtraSymbolError'>
```

**exception** `tt.errors.symbols.MissingSymbolError` (*message*, \**args*)

Bases: `tt.errors.symbols.SymbolError`

An exception type for a missing token value in evaluation.

```
>>> from tt import BooleanExpression
>>> try:
...     b = BooleanExpression('A and B')
...     b.evaluate(A=1)
... except Exception as e:
...     print(type(e))
...
<class 'tt.errors.symbols.MissingSymbolError'>
```

**exception** `tt.errors.symbols.SymbolError` (*message*, \**args*)

Bases: `tt.errors.base.TtError`

An exception for errors occurring in symbol processing.

---

**Note:** This exception type should be sub-classed and is not meant to be raised explicitly.

---

## expressions

Tools for working with Boolean expressions.

### `expressions.bexpr` module

Tools for interacting with Boolean expressions.

**class** `tt.expressions.bexpr.BooleanExpression` (*expr*)

Bases: `object`

An interface for interacting with a Boolean expression.

Instances of `BooleanExpression` are meant to be immutable and can be instantiated from a few different representations of expressions. The simplest way to make an expression object is from a string:

```
>>> from tt import BooleanExpression
>>> BooleanExpression('(A or B) iff (C and D)')
<BooleanExpression "(A or B) iff (C and D)">
```

If you already have an instance of `ExpressionTreeNode` laying around, you can make a new expression object from that, too:

```
>>> from tt import ExpressionTreeNode
>>> tree_root = ExpressionTreeNode.build_tree(
...     ['A', 'B', 'or',
...      'C', 'D', 'and',
...      'iff'])
>>> BooleanExpression(tree_root)
<BooleanExpression "(A or B) iff (C and D)">
```

Additionally, any sub-tree node can be used to build an expression object. Continuing from above, let's make a new expression object for each of the sub-expressions wrapped in parentheses:



```
>>> BooleanExpression(tree_root.l_child)
<BooleanExpression "A or B">
>>> BooleanExpression(tree_root.r_child)
<BooleanExpression "C and D">
```

Expressions also implement the equality and inequality operators (`==` and `!=`). Equality is determined by the same semantic structure and the same operand names; the string used to represent the operators in two expressions is not taken into account. Here's a few examples:

```
>>> from tt import BooleanExpression as be
>>> be('A or B or C') == be('A or B or C')
True
>>> be('A or B or C') == be('A || B || C')
True
>>> be('A or B or C') == be('A or C or B')
False
```

**Parameters** `expr` (`str` or `ExpressionTreeNode`) – The expression representation from which this object is derived.

#### Raises

- ***BadParenPositionError*** – If the passed expression contains a parenthesis in an invalid position.
- ***EmptyExpressionError*** – If the passed expressions contains nothing other than whitespace.
- ***ExpressionOrderError*** – If the expression contains invalid consecutive operators or operands.
- ***InvalidArgumentTypeError*** – If `expr` is not an acceptable type.
- ***InvalidIdentifierError*** – If any parsed variable symbols in the expression are invalid identifiers.
- ***UnbalancedParenError*** – If any parenthesis pairs remain unbalanced.

It is important to note that aside from *InvalidArgumentTypeError*, all exceptions raised in expression initialization will be descendants of *GrammarError*.

#### **constrain** (`**kwargs`)

A context manager to impose satisfiability constraints.

This is the interface for adding assumptions to the satisfiability solving functionality provided through the `sat_one()` and `sat_all()` methods.

It should be noted that this context manager is only designed to work with the satisfiability-related functionality of this class. Constrained symbol values will not have an effect on non-sat methods of this class. For example:

```
>>> from tt import BooleanExpression
>>> b = BooleanExpression('(A or B) and (C or D)')
>>> with b.constrain(A=1):
...     b.evaluate(A=0, B=1, C=1, D=0)
...
True
```

This context manager returns a reference to the same object upon which it is called. This behavior is designed with the following use case in mind:

```

>>> from tt import BooleanExpression
>>> with BooleanExpression('A or B').constrain(A=1, B=0) as b:
...     b.sat_one()
...
<BooleanValues [A=1, B=0]>

```

**Parameters** *kwargs* – Keys are names of symbols in this expression; the specified value for each of these keys will be added to the `constraints` attribute of this object for the duration of the context manager.

**Returns** A reference to the same object that called this method (i.e., `self` in the context of this method).

**Return type** *BooleanExpression*

**Raises**

- *AlreadyConstrainedSymbolError* – If trying to constrain this expression with multiple context managers.
- *ExtraSymbolError* – If a symbol not in this expression is passed through `kwargs`.
- *InvalidArgumentValueError* – If no constraints are specified (i.e., `kwargs` is empty).
- *InvalidBooleanValueError* – If any values from `kwargs` are not valid Boolean inputs.

**evaluate** (*\*\*kwargs*)

Evaluate the Boolean expression for the passed keyword arguments.

This is a checked wrapper around the `evaluate_unchecked()` function.

**Parameters** *kwargs* – Keys are names of symbols in this expression; the specified value for each of these keys will be substituted into the expression for evaluation.

**Returns** The result of evaluating the expression.

**Return type** `bool`

**Raises**

- *ExtraSymbolError* – If a symbol not in this expression is passed through `kwargs`.
- *MissingSymbolError* – If any symbols in this expression are not passed through `kwargs`.
- *InvalidBooleanValueError* – If any values from `kwargs` are not valid Boolean inputs.
- *InvalidIdentifierError* – If any symbol names are invalid identifiers.

Usage:

```

>>> from tt import BooleanExpression
>>> b = BooleanExpression('A or B')
>>> b.evaluate(A=0, B=0)
False
>>> b.evaluate(A=1, B=0)
True

```

**evaluate\_unchecked** (\*\*kwargs)

Evaluate the Boolean expression without checking the input.

This is used for evaluation by the `evaluate()` method, which validates the input `kwargs` before passing them to this method.

**Parameters** `kwargs` – Keys are names of symbols in this expression; the specified value for each of these keys will be substituted into the expression for evaluation.

**Returns** The Boolean result of evaluating the expression.

**Return type** `bool`

**is\_cnf**

Whether this expression is in conjunctive normal form or not.

**Type** `bool`

```
>>> from tt import BooleanExpression
>>> b = BooleanExpression('(A or ~B) and (~C or D or E) and F')
>>> b.is_cnf
True
>>> b = BooleanExpression('A nand B')
>>> b.is_cnf
False
```

**is\_dnf**

Whether this expression is in conjunctive normal form or not.

**Type** `bool`

```
>>> from tt import BooleanExpression
>>> b = BooleanExpression('(A and B) or (~C and D)')
>>> b.is_dnf
True
>>> b = BooleanExpression('(op1 or !op2) and (op3 or op4)')
>>> b.is_dnf
False
```

**iter\_clauses** ()

Iterate over the clauses in this expression.

An expression must be in conjunctive normal form (CNF) or disjunctive normal form (DNF) in order to iterate over its clauses. Here's a simple example:

```
>>> from tt import BooleanExpression
>>> b = BooleanExpression('(~A or B) and (C or D) and (~E or ~F)')
>>> for clause in b.iter_clauses():
...     clause
...
<BooleanExpression "~A or B">
<BooleanExpression "C or D">
<BooleanExpression "~E or ~F">
```

In the case of an ambiguous expression form (between CNF and DNF), the clauses will be interpreted to be in CNF form. For example:

```
>>> b = BooleanExpression('A and ~B and C')
>>> b.is_cnf
True
>>> b.is_dnf
```

```
True
>>> print(', '.join(str(clause) for clause in b.iter_clauses()))
A, ~B, C
```

If you want to enforce a specific CNF or DNF interpretation of the clauses, take a look at `iter_cnf_clauses()` and `iter_dnf_clauses()`.

**Returns** An iterator of expression objects, each representing a separate clause of this expression.

**Return type** `Iterator[BooleanExpression]`

**Raises** `RequiresNormalFormError` – If this expression is not in conjunctive or disjunctive normal form.

#### `iter_cnf_clauses()`

Iterate over the CNF clauses in this expression.

```
>>> from tt import BooleanExpression
>>> b = BooleanExpression('(A or B) and ~C')
>>> for clause in b.iter_cnf_clauses():
...     print(clause)
...
A or B
~C
```

**Returns** An iterator of expression objects, each representing a separate CNF clause of this expression.

**Return type** `Iterator[BooleanExpression]`

**Raises** `RequiresNormalFormError` – If this expression is not in conjunctive normal form.

#### `iter_dnf_clauses()`

Iterate over the DNF clauses in this expression.

```
>>> from tt import BooleanExpression
>>> b = BooleanExpression('(A and ~B) or (C and D and E)')
>>> for clause in b.iter_dnf_clauses():
...     print(clause)
...
A and ~B
C and D and E
```

**Returns** An iterator of expression objects, each representing a separate DNF clause of this expression.

**Return type** `Iterator[BooleanExpression]`

**Raises** `RequiresNormalFormError` – If this expression is not in disjunctive normal form.

#### `postfix_tokens`

Similar to the `tokens` attribute, but in postfix order.

**Type** `List[str]`

```
>>> from tt import BooleanExpression
>>> b = BooleanExpression('A xor (B or C)')
>>> b.postfix_tokens
['A', 'B', 'C', 'or', 'xor']
```

**raw\_expr**

The raw string expression, parsed upon initialization.

This is what you pass into the `BooleanExpression` constructor; it is kept on the object as an attribute for convenience.

**Type** `str`

```
>>> from tt import BooleanExpression
>>> b = BooleanExpression('A nand B')
>>> b.raw_expr
'A nand B'
```

**sat\_all()**

Find all combinations of inputs that satisfy this expression.

Under the hood, this method is using the functionality exposed in tt's `satisfiability.picosat` module.

Here's a simple example of iterating through a few SAT solutions:

```
>>> from tt import BooleanExpression
>>> b = BooleanExpression('(A xor B) and (C xor D)')
>>> for solution in b.sat_all():
...     print(solution)
...
A=0, B=1, C=0, D=1
A=0, B=1, C=1, D=0
A=1, B=0, C=1, D=0
A=1, B=0, C=0, D=1
```

We can also constrain away a few of those solutions:

```
>>> with b.constrain(A=1, C=0):
...     for solution in b.sat_all():
...         print(solution)
...
A=1, B=0, C=0, D=1
```

**Returns** An iterator of `namedtuple`-like objects representing satisfying combinations of inputs; if no satisfying solutions exist, the iterator will be empty.

**Return type** `Iterator[namedtuple-like objects]`

**Raises** `NoEvaluationVariationError` – If this is an expression of only constants.

**sat\_one()**

Find a combination of inputs that satisfies this expression.

Under the hood, this method is using the functionality exposed in tt's `satisfiability.picosat` module.

Here's a simple example of satisfying an expression:

```
>>> from tt import BooleanExpression
>>> b = BooleanExpression('A xor 1')
>>> b.sat_one()
<BooleanValues [A=0]>
```

Don't forget about the utility provided by the `constrain()` context manager:

```
>>> b = BooleanExpression('(A nand B) iff C')
>>> with b.constrain(A=1, C=1):
...     b.sat_one()
...
<BooleanValues [A=1, B=0, C=1]>
```

Finally, here's an example when the expression cannot be satisfied:

```
>>> with BooleanExpression('A xor 1').constrain(A=1) as b:
...     b.sat_one() is None
...
True
```

**Returns** `namedtuple`-like object representing a satisfying set of values (see `boolean_variables_factory` for more information about the type of object returned); `None` will be returned if no satisfiable set of inputs exists.

**Return type** `namedtuple`-like object or `None`

**Raises** `NoEvaluationVariationError` – If this is an expression of only constants.

### symbols

The list of unique symbols present in this expression.

The order of the symbols in this list matches the order of symbol appearance in the original expression.

**Type** `List[str]`

```
>>> from tt import BooleanExpression
>>> b = BooleanExpression('A xor (B or C)')
>>> b.symbols
['A', 'B', 'C']
```

### tokens

The parsed, non-whitespace tokens of an expression.

**Type** `List[str]`

```
>>> from tt import BooleanExpression
>>> b = BooleanExpression('A xor (B or C)')
>>> b.tokens
['A', 'xor', '(', 'B', 'or', 'C', ')']
```

### tree

The tree node representing the root of the tree of this expression.

**Type** `ExpressionTreeNode`

```
>>> from tt import BooleanExpression
>>> b = BooleanExpression('A xor (B or C)')
>>> print(b.tree)
xor
 \----A
 \----or
      \----B
      \----C
```

## satisfiability

Functionality for determining logic satisfiability.

### satisfiability.picosat module

Python wrapper around the `_clibs` PicoSAT extension.

`tt.satisfiability.picosat.sat_all` (*clauses*, *assumptions=None*)

Find all solutions that satisfy the specified clauses and assumptions.

This provides a light Python wrapper around the same method in the PicoSAT C-extension. While completely tested and usable, this method is probably not as useful as the interface provided through the `sat_all` method in the `BooleanExpression` class.

#### Parameters

- **clauses** (List[List[int]]) – CNF (AND of ORs) clauses; positive integers represent non-negated terms and negative integers represent negated terms.
- **assumptions** (List[int]) – Assumed terms; same negation logic from `clauses` applies here. Note that assumptions *cannot* be an empty list; leave it as `None` if there are no assumptions to include.

**Returns** An iterator of solutions; if no satisfiable solutions exist, the iterator will be empty.

**Return type** Iterator[List[int]]

#### Raises

- **InvalidArgumentTypeError** – If `clauses` is not a list of lists of ints or `assumptions` is not a list of ints.
- **InvalidArgumentValueError** – If any literal ints are equal to zero.

Here's an example showing the basic usage:

```
>>> from tt import picosat
>>> for solution in picosat.sat_all([[1], [2, 3, 4], [2, 3]]):
...     print(solution)
...
[1, 2, 3, 4]
[1, 2, 3, -4]
[1, 2, -3, 4]
[1, 2, -3, -4]
[1, -2, 3, 4]
[1, -2, 3, -4]
```

We can cut down on some of the above solutions by including an assumption:

```
>>> for solution in picosat.sat_all([[1], [2, 3, 4], [2, 3]],
...                                 assumptions=[-3]):
...     print(solution)
...
[1, 2, -3, 4]
[1, 2, -3, -4]
```

`tt.satisfiability.picosat.sat_one` (*clauses*, *assumptions=None*)

Find a solution that satisfies the specified clauses and assumptions.

This provides a light Python wrapper around the same method in the PicoSAT C-extension. While completely tested and usable, this method is probably not as useful as the interface provided through the `sat_one` method in the `BooleanExpression` class.

### Parameters

- **clauses** (List[List[int]]) – CNF (AND of ORs) clauses; positive integers represent non-negated terms and negative integers represent negated terms.
- **assumptions** (List[int]) – Assumed terms; same negation logic from `clauses` applies here. Note that assumptions *cannot* be an empty list; leave it as `None` if there are no assumptions to include.

**Returns** If solution is found, a list of ints representing the terms of the solution; otherwise, if no solution found, `None`.

**Return type** List[int] or None

### Raises

- **InvalidArgumentTypeError** – If `clauses` is not a list of lists of ints or `assumptions` is not a list of ints.
- **InvalidArgumentValueError** – If any literal ints are equal to zero.

Let's look at a simple example with no satisfiable solution:

```
>>> from tt import picosat
>>> picosat.sat_one([[1], [-1]]) is None
True
```

Here's an example where a solution exists:

```
>>> picosat.sat_one([[1, 2, 3], [-2, -3], [1, -2], [2, -3], [-2]])
[1, -2, -3]
```

Finally, here's an example using assumptions:

```
>>> picosat.sat_one([[1, 2, 3], [2, 3]], assumptions=[-1, -3])
[-1, 2, -3]
```

## tables

Tools for working with truth tables.

### tables.truth\_table module

Implementation of a truth table.

**class** `tt.tables.truth_table.TruthTable` (*expr=None, from\_values=None, fill\_all=True, ordering=None*)

Bases: `object`

A class representing a truth table.

There are two ways to fill a table: either populated from an expression or by specifying the values yourself.

An existing `BooleanExpression` expression can be used, or you can just pass in a string:



```

>>> from tt import TruthTable
>>> t = TruthTable('A xor B')
>>> print(t)
+----+----+----+
| A | B |   |
+----+----+----+
| 0 | 0 | 0 |
+----+----+----+
| 0 | 1 | 1 |
+----+----+----+
| 1 | 0 | 1 |
+----+----+----+
| 1 | 1 | 0 |
+----+----+----+

```

When manually specifying the values tt can generate the symbols for you:

```

>>> from tt import TruthTable
>>> t = TruthTable(from_values='0110')
>>> print(t)
+----+----+----+
| A | B |   |
+----+----+----+
| 0 | 0 | 0 |
+----+----+----+
| 0 | 1 | 1 |
+----+----+----+
| 1 | 0 | 1 |
+----+----+----+
| 1 | 1 | 0 |
+----+----+----+

```

You can also specify the symbol names yourself, if you'd like:

```

>>> from tt import TruthTable
>>> t = TruthTable(from_values='0110', ordering=['tt', 'rocks'])
>>> print(t)
+----+-----+----+
| tt | rocks |   |
+----+-----+----+
| 0 | 0 | 0 |
+----+-----+----+
| 0 | 1 | 1 |
+----+-----+----+
| 1 | 0 | 1 |
+----+-----+----+
| 1 | 1 | 0 |
+----+-----+----+

```

### Parameters

- **expr** (*str* or *BooleanExpression*) – The expression with which to populate this truth table. If this argument is omitted, then the `from_values` argument must be properly set.
- **from\_values** (*str*) – A string of 1's, 0's, and x's representing the values to be stored in the table; the length of this string must be a power of 2 and is the complete set of values (in sequential order) to be stored in table.

- **fill\_all** (`bool`, optional) – A flag indicating whether the entirety of the table should be filled on initialization; defaults to `True`.
- **ordering** (`List[str]`, optional) – An input that maps to this class’s `ordering` property. If omitted, the ordering of symbols in the table will match that of the symbols’ appearance in the original expression.

#### Raises

- **ConflictingArgumentsError** – If both `expr` and `from_values` are specified in the initialization; a table can only be instantiated from one or the other.
- **DuplicateSymbolError** – If multiple symbols of the same name are passed into the `ordering` list.
- **ExtraSymbolError** – If a symbol not present in the expression is passed into the `ordering` list.
- **MissingSymbolError** – If a symbol present in the expression is omitted from the `ordering` list.
- **InvalidArgumentTypeError** – If an unexpected parameter type is encountered.
- **InvalidArgumentValueError** – If the number of values specified via `from_values` is not a power of 2 or the `ordering` list (when filling the table using `from_values`) is empty.
- **InvalidIdentifierError** – If any symbol names specified in `ordering` are not valid identifiers.
- **NoEvaluationVariationError** – If an expression without any unique symbols (i.e., one merely composed of constant operands) is specified.
- **RequiredArgumentError** – If neither the `expr` or `from_values` arguments are specified.

#### `equivalent_to` (*other*)

Return whether this table is equivalent to another source of truth.

**Parameters** `other` (*TruthTable*, *str*, or *BooleanExpression*) – The other source of truth with which to compare logical equivalence.

**Returns** `True` if the other expression is logically equivalent to this one, otherwise `False`.

**Return type** `bool`

#### Raises

- **InvalidArgumentTypeError** – If the `other` argument is not one of the acceptable types.
- **RequiresFullTableError** – If either the calling table or other source of truth represents an unfilled table.

It is important to note that the concept of equivalence employed here is only concerned with the corresponding outputs between this table and the other provided source of truth. For example, the ordering of symbols is not taken into consideration when computing equivalence:

```
>>> from tt import TruthTable
>>> t1 = TruthTable('op1 or op2')
>>> t2 = TruthTable('A or B')
>>> t1.equivalent_to(t2)
True
```

```
>>> t2.equivalent_to(t1)
True
```

Another area of possible ambiguity here is the role of the don't care value in equivalence. When comparing tables, don't cares in the caller will allow for any corresponding value in *other*, but the reverse is not true. For example:

```
>>> from tt import TruthTable
>>> t1 = TruthTable(from_values='0x11')
>>> t2 = TruthTable(from_values='0011')
>>> t1.equivalent_to(t2)
True
>>> t2.equivalent_to(t1)
False
```

Additionally, only full tables are valid for equivalence checks. The appropriate error will be raised if you attempt to check the equivalence of partially filled tables:

```
>>> from tt import TruthTable
>>> t = TruthTable('A or B', fill_all=False)
>>> t.fill(A=0)
>>> try:
...     t.equivalent_to('A or B')
... except Exception as e:
...     print(type(e))
...
<class 'tt.errors.state.RequiresFullTableError'>
```

#### **expr**

The BooleanExpression object represented by this table.

This attribute will be None if this table was not derived from an expression (i.e., the user provided the values).

**Type** *BooleanExpression*

#### **fill** (*\*\*kwargs*)

Fill the table with results, based on values specified by *kwargs*.

**Parameters** *kwargs* – Filter which entries in the table are filled by specifying symbol values through the keyword args.

#### **Raises**

- *AlreadyFullTableError* – If the table is already full when this method is called.
- *ExtraSymbolError* – If a symbol not in the expression is passed as a keyword arg.
- *InvalidBooleanValueError* – If a non-Boolean value is passed as a value for one of the keyword args.

An example of iteratively filling a table:

```
>>> from tt import TruthTable
>>> t = TruthTable('A or B', fill_all=False)
>>> print(t)
Empty!
>>> t.fill(A=0)
>>> print(t)
+----+----+----+
```

```

| A | B |   |
+---+---+---+
| 0 | 0 | 0 |
+---+---+---+
| 0 | 1 | 1 |
+---+---+---+
>>> t.fill(A=1)
>>> print(t)
+---+---+---+
| A | B |   |
+---+---+---+
| 0 | 0 | 0 |
+---+---+---+
| 0 | 1 | 1 |
+---+---+---+
| 1 | 0 | 1 |
+---+---+---+
| 1 | 1 | 1 |
+---+---+---+

```

**static generate\_symbols** (*num\_symbols*)

Generate a list of symbols for a specified number of symbols.

Generated symbol names are permutations of a properly-sized number of uppercase alphabet letters.

**Parameters** *num\_symbols* (*int*) – The number of symbols to generate.

**Returns** A list of strings of length *num\_symbols*, containing auto-generated symbols.

**Return type** List[str]

A simple example:

```

>>> from tt import TruthTable
>>> TruthTable.generate_symbols(3)
['A', 'B', 'C']
>>> TruthTable.generate_symbols(7)
['A', 'B', 'C', 'D', 'E', 'F', 'G']

```

**static input\_combos** (*combo\_len*)

Get an iterator of Boolean input combinations for this expression.

**Parameters** *combo\_len* (*int*, optional) – The length of each combination in the returned iterator.

**Returns** An iterator of tuples containing permutations of Boolean inputs.

**Return type** *itertools.product*

A simple example:

```

>>> from tt import TruthTable
>>> for tup in TruthTable.input_combos(2):
...     print(tup)
...
(False, False)
(False, True)
(True, False)
(True, True)

```

**is\_full**

A Boolean flag indicating whether this table is full or not.

**Type** `bool`

Attempting to further fill an already-full table will raise an *AlreadyFullTableError*:

```
>>> from tt import TruthTable
>>> t = TruthTable('A or B', fill_all=False)
>>> t.is_full
False
>>> t.fill()
>>> t.is_full
True
>>> try:
...     t.fill()
... except Exception as e:
...     print(type(e))
...
<class 'tt.errors.state.AlreadyFullTableError'>
```

**ordering**

The order in which the symbols should appear in the truth table.

**Type** `List[str]`

Here's a short example of alternative orderings of a partially-filled, three-symbol table:

```
>>> from tt import TruthTable
>>> t = TruthTable('(A or B) and C', fill_all=False)
>>> t.fill(A=0, B=0)
>>> print(t)
+---+---+---+---+
| A | B | C |   |
+---+---+---+---+
| 0 | 0 | 0 | 0 |
+---+---+---+---+
| 0 | 0 | 1 | 0 |
+---+---+---+---+
>>> t = TruthTable('(A or B) and C',
...                 fill_all=False, ordering=['C', 'B', 'A'])
>>> t.fill(A=0, B=0)
>>> print(t)
+---+---+---+---+
| C | B | A |   |
+---+---+---+---+
| 0 | 0 | 0 | 0 |
+---+---+---+---+
| 1 | 0 | 0 | 0 |
+---+---+---+---+
```

**results**

A list containing the results of each possible set of inputs.

**Type** `List[bool, str]`

In the case that the table is not completely filled, spots in this list that do not yet have a computed result will hold the `None` value.

Regardless of the filled status of this table, all positions in the `results` list are allocated at initialization and subsequently filled as computed. This is illustrated in the below example:

```

>>> from tt import TruthTable
>>> t = TruthTable('A or B', fill_all=False)
>>> t.results
[None, None, None, None]
>>> t.fill(A=0)
>>> t.results
[False, True, None, None]
>>> t.fill()
>>> t.results
[False, True, True, True]

```

If the table is filled upon initialization via the `from_values` parameter, don't care strings could be present in the result list:

```

>>> from tt import TruthTable
>>> t = TruthTable(from_values='1xx0')
>>> t.results
[True, 'x', 'x', False]

```

## transformations

Interfaces for transforming representations of expressions.

### transformations.bexpr module

Transformation functions for expressions.

`tt.transformations.bexpr.apply_de_morgans` (*expr*)

Convert an expression to a form with De Morgan's Law applied.

**Returns** A new expression object, transformed so that De Morgan's Law has been applied to negated *ANDs* and *ORs*.

**Return type** *BooleanExpression*

**Raises** *InvalidArgumentTypeError* – If *expr* is not a valid type.

Here's a couple of simple examples showing De Morgan's Law being applied to a negated AND and a negated OR:

```

>>> from tt import apply_de_morgans
>>> apply_de_morgans(r'~(A /\ B)')
<BooleanExpression "~A \/ ~B">
>>> apply_de_morgans(r'~(A \/ B)')
<BooleanExpression "~A /\ ~B">

```

`tt.transformations.bexpr.coalesce_negations` (*expr*)

Convert an expression to a form with all negations condensed.

**Returns** A new expression object, transformed so that all “runs” of logical *NOTs* are condensed into the minimal equivalent number.

**Return type** *BooleanExpression*

**Raises** *InvalidArgumentTypeError* – If *expr* is not a valid type.

Here's a simple example showing the basic premise of this transformation:

```
>>> from tt import coalesce_negations
>>> coalesce_negations('~A or ~B or ~~~C or ~~~~D')
<BooleanExpression "A or ~B or ~C or D">
```

This transformation works on expressions, too:

```
>>> coalesce_negations('!!(A -> not not B) or ~(~(A xor B))')
<BooleanExpression "(A -> B) or (A xor B)">
```

`tt.transformations.bexpr.distribute_and` (*expr*)

Convert an expression to distribute ANDs over ORed clauses.

**Parameters** *expr* (*str* or *BooleanExpression*) – The expression to transform.

**Returns** A new expression object, transformed to distribute ANDs over ORed clauses.

**Return type** *BooleanExpression*

**Raises** *InvalidArgumentTypeError* – If *expr* is not a valid type.

Here's a couple of simple examples:

```
>>> from tt import distribute_and
>>> distribute_and('A and (B or C or D)')
<BooleanExpression "(A and B) or (A and C) or (A and D)">
>>> distribute_and('(A or B) and C')
<BooleanExpression "(A and C) or (B and C)">
```

And an example involving distributing a sub-expression:

```
>>> distribute_and('(A and B) and (C or D or E)')
<BooleanExpression "(A and B and C) or (A and B and D) or (A and B and E)">
```

`tt.transformations.bexpr.distribute_or` (*expr*)

Convert an expression to distribute ORs over ANDed clauses.

**Parameters** *expr* (*str* or *BooleanExpression*) – The expression to transform.

**Returns** A new expression object, transformed to distribute ORs over ANDed clauses.

**Return type** *BooleanExpression*

**Raises** *InvalidArgumentTypeError* – If *expr* is not a valid type.

Here's a couple of simple examples:

```
>>> from tt import distribute_or
>>> distribute_or('A or (B and C and D and E)')
<BooleanExpression "(A or B) and (A or C) and (A or D) and (A or E)">
>>> distribute_or('(A and B) or C')
<BooleanExpression "(A or C) and (B or C)">
```

And an example involving distributing a sub-expression:

```
>>> distribute_or('(A or B) or (C and D)')
<BooleanExpression "(A or B or C) and (A or B or D)">
```

`tt.transformations.bexpr.to_cnf` (*expr*)

Convert an expression to conjunctive normal form (CNF).

This transformation only guarantees to produce an equivalent form of the passed expression in conjunctive normal form; the transformed expression may be an inefficient representation of the passed expression.

**Parameters** `expr` (`str` or `BooleanExpression`) – The expression to transform.

**Returns** A new expression object, transformed to be in CNF.

**Return type** `BooleanExpression`

**Raises** `InvalidArgumentTypeError` – If `expr` is not a valid type.

Here are a few examples:

```
>>> from tt import to_cnf
>>> b = to_cnf('(A nor B) impl C')
>>> b
<BooleanExpression "A or B or C">
>>> b.is_cnf
True
>>> b = to_cnf(r'~(~(A /\ B) /\ C /\ D)')
>>> b
<BooleanExpression "(A \/ ~C \/ ~D) /\ (B \/ ~C \/ ~D)">
>>> b.is_cnf
True
```

`tt.transformations.bexpr.to_primitives(expr)`

Convert an expression to a form with only primitive operators.

All operators will be transformed equivalent form composed only of the logical AND, OR, and NOT operators. Symbolic operators in the passed expression will remain symbolic in the transformed expression and the same applies for plain English operators.

**Parameters** `expr` (`str` or `BooleanExpression`) – The expression to transform.

**Returns** A new expression object, transformed to contain only primitive operators.

**Return type** `BooleanExpression`

**Raises** `InvalidArgumentTypeError` – If `expr` is not a valid type.

Here's a simple transformation of exclusive-or:

```
>>> from tt import to_primitives
>>> to_primitives('A xor B')
<BooleanExpression "(A and not B) or (not A and B)">
```

And another example of if-and-only-if (using symbolic operators):

```
>>> to_primitives('A <-> B')
<BooleanExpression "(A /\ B) \/ (~A /\ ~B)">
```

## trees

Tools for working with Boolean expression trees.

### `trees.tree_node` module

A node, and related classes, for use in expression trees.



**class** `tt.trees.tree_node.BinaryOperatorExpressionTreeNode` (*operator\_str*, *l\_child*, *r\_child*)

Bases: `tt.trees.tree_node.ExpressionTreeNode`

An expression tree node for binary operators.

**operator**

The actual operator object wrapped in this node.

**Type** `BooleanOperator`

**class** `tt.trees.tree_node.ExpressionTreeNode` (*symbol\_name*, *l\_child=None*, *r\_child=None*)

Bases: `object`

A base class for expression tree nodes.

This class is extended within `tt` and is not meant to be used directly.

If you plan to extend it, note that descendants of this class must compute the `_is_cnf`, `_is_dnf`, and `_is_really_unary` boolean attributes within their initialization. Additionally, descendants of this class must implement the `__eq__` magic method (but not `__ne__`).

**apply\_de\_morgans** ()

Return a transformed node, with De Morgan's Law applied.

Since nodes are immutable, the returned node, and all descendants, are new objects.

**Returns** An expression tree node with all negated AND and OR operators transformed, following De Morgan's Law.

**Return type** `ExpressionTreeNode`

**static build\_tree** (*postfix\_tokens*)

Build a tree from a list of expression tokens in postfix order.

This method does not check that the tokens are indeed in postfix order; undefined behavior will ensue if you pass tokens in an order other than postfix.

**Parameters** `postfix_tokens` (`List[str]`) – A list of string tokens from which to construct the tree of expression nodes.

**Returns** The root node of the constructed tree.

**Return type** `ExpressionTreeNode`

**Raises**

- `InvalidArgumentTypeError` – If `postfix_tokens` is not a list of strings.
- `InvalidArgumentValueError` – If `postfix_tokens` is empty.

**coalesce\_negations** ()

Return a transformed node, with consecutive negations coalesced.

Since nodes are immutable, the returned node, and all descendants, are new objects.

**Returns** An expression tree node with all consecutive negations compressed into the minimal number of equivalent negations (either one or none).

**Return type** `ExpressionTreeNode`

**distribute\_and** ()

Return a transformed nodes, with ANDs recursively distributed across ORed sub-expressions.

Since nodes are immutable, the returned node, and all descendants, are new objects.

**Returns** An expression tree node with all applicable AND operators distributed across ORed sub-expressions.

**Return type** *ExpressionTreeNode*

**distribute\_ors** ()

Return a transformed nodes, with ORs recursively distributed across ANDED sub-expressions.

Since nodes are immutable, the returned node, and all descendants, are new objects.

**Returns** An expression tree node with all applicable OR operators distributed across ANDED sub-expressions.

**Return type** *ExpressionTreeNode*

**evaluate** (*input\_dict*)

Recursively evaluate this node.

This is an interface that should be defined in sub-classes. Node evaluation does no checking of the validity of inputs; they should be check before being passed here.

**Parameters** **input\_dict** (Dict{*str*: *truthy*}) – A dictionary mapping expression symbols to the value for which they should be substituted in expression evaluation.

**Returns** The evaluation of the tree rooted at this node.

**Return type** *bool*

**is\_cnf**

Whether the tree rooted at this node is in conjunctive normal form.

**Type** *bool*

**is\_dnf**

Whether the tree rooted at this node is in disjunctive normal form.

**Type** *bool*

**is\_really\_unary**

Whether the tree rooted at this node contains no binary operators.

**Type** *bool*

**iter\_clauses** ()

Iterate the clauses in the expression tree rooted at this node.

If the normal form of the expression is ambiguous, then precedence will be given to conjunctive normal form.

**Returns** Iterator of each CNF or DNF clause, rooted by a tree node, contained within the expression tree rooted at this node.

**Return type** Iterator[*ExpressionTreeNode*]

**Raises** *RequiresNormalFormError* – If this expression is not in conjunctive or disjunctive normal form.

**iter\_cnf\_clauses** ()

Iterate the clauses in conjunctive normal form order.

**Returns** Iterator of each CNF clause, rooted by a tree node, contained within the expression tree rooted at this node.

**Return type** Iterator[*ExpressionTreeNode*]

**Raises** *RequiresNormalFormError* – If the expression tree rooted at this node is not in conjunctive normal form.

**iter\_dnf\_clauses** ()

Iterate the clauses in disjunctive normal form order.

**Returns** Iterator of each DNF clause, rooted by a tree node, contained within the expression tree rooted at this node.

**Return type** *Iterator[ExpressionTreeNode]*

**Raises** *RequiresNormalFormError* – If the expression tree rooted at this node is not in disjunctive normal form.

**l\_child**

This node's left child; *None* indicates the absence of a child.

**Type** *ExpressionTreeNode* or *None*

**r\_child**

This node's right child; *None* indicates the absence of a child.

**Type** *ExpressionTreeNode* or *None*

**symbol\_name**

The string operator/operand name wrapped in this node.

**Type** *str*

**to\_cnf** ()

Return a transformed node, in conjunctive normal form.

Since nodes are immutable, the returned node, and all descendants, are new objects.

**Returns** An expression tree node with all operators transformed to consist only of NOTs, ANDs, and ORs.

**Return type** *ExpressionTreeNode*

**to\_primitives** ()

Return a transformed node, containing only NOTs, ANDs, and ORs.

Since nodes are immutable, the returned node, and all descendants, are new objects.

**Returns** An expression tree node with all operators transformed to consist only of NOTs, ANDs, and ORs.

**Return type** *ExpressionTreeNode*

**class** `tt.trees.tree_node.OperandExpressionTreeNode` (*operand\_str*)

Bases: *tt.trees.tree\_node.ExpressionTreeNode*

An expression tree node for operands.

Nodes of this type will always be leaves in an expression tree.

**class** `tt.trees.tree_node.UnaryOperatorExpressionTreeNode` (*operator\_str, l\_child*)

Bases: *tt.trees.tree\_node.ExpressionTreeNode*

An expression tree node for unary operators.

**operator**

The actual operator object wrapped in this node.

**Type** *BooleanOperator*



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